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Centre number		Candidate number	
Surname			
Forename(s)			
Candidate signature			

GCSE MATHEMATICS

H

Higher Tier

Paper 2 Calculator

Thursday 7 November 2019 Morning Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- a calculator
- · mathematical instruments.



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper.
 These must be tagged securely to this answer book.

Advice

In all calculations, show clearly how you work out your answer.



For Examiner's Use		
Pages	Mark	
2–3		
4–5		
6–7		
8–9		
10–11		
12–13		
14–15		
16–17		
18–19		
20–21		
22–23		
24–25		
TOTAL		

Please note that these worked solutions have neither been provided nor approved by AQA and may not necessarily constitute the only possible solutions. Please refer to the original mark schemes for full guidance.

Any writing in blue indicates what must be written in the exam.

Anything written in green in a rectangle doesn't have to be written in the exam.

If you find any mistakes or have any requests or suggestions, please send an email to curtis@cgmaths.co.uk

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Answer all questions in the spaces provided

1 Expand Circle your answer.

[1 mark]

 $32x^{3}$

$$12x^3 + 20x^2$$

$$7x^3 + 9x^2$$
 $12x^2 + 5$

$$12x^2 + 5$$

$$4x^2 \times 3x = 4 \times 3 \times x^2 \times x = 12x^3$$

 $4x^2 \times 5 = 4 \times 5 \times x^2 = 20x^2$

2 How many millimetres are there in a kilometre? Circle your answer.

[1 mark]

10³

10⁵



10⁹

 $\frac{7}{12}$ and $\frac{3}{4}$ Circle the number half way between 3

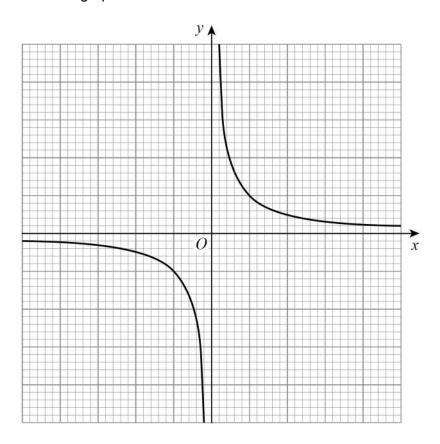
[1 mark]

32

$$\frac{2}{3}$$

Doing the mean of the two fractions works out what is half way. 7/12 + 3/4 = 4/3 $4/3 \div 2 = 2/3$

4 Here is the sketch of a graph.



Circle the equation of the graph.

[1 mark]

$$y = x$$

$$y = -x^2 \qquad \qquad y = -x^3$$

$$y = -x^3$$

$$y = \frac{1}{x}$$

This is a typical graph so is one which might be known. Otherwise table mode could be used on the calculator to do a table of values for each equation. y = 1/x is the only one which would have this shape

Work out the lowest common multiple (LCM) of 120 and 144

[2 marks]

$$120 = 2^3 \times 3 \times 5$$

 $144 = 2^4 \times 3^2$

Expressing both 120 and 144 as a product of prime factors. The calculator can be used to do this

2⁴×3²×5 ←

The lowest common multiple is the highest power of each prime in both lists multiplied together

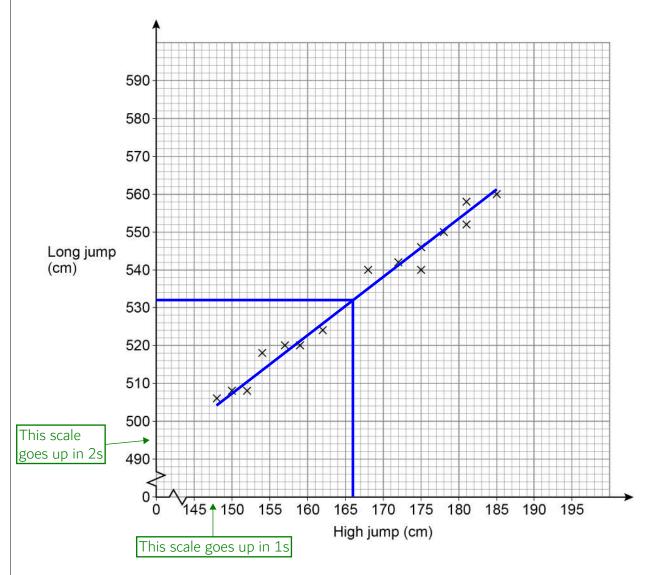
Newer versions of Casio calculators can work out the lowest common multiple without having to do this method

Answer

720



6 The scatter graph shows the best high jump and the best long jump for 15 boys.



6 (a) Write down the type of correlation shown.

[1 mark]

Answer	Positive

As one variable (the high jump) increases, so does the other variable (the long jump). So this is positive correlation



6 (b) Liam has a best high jump of 166 cm

Use a line of best fit to estimate his best long jump.

[2 marks]

Answer 532 cm

Drawing a line of best fit using a clear ruler by trying to get the same amount of points above and below the line and have it going in the same direction as the points. Then reading up from 166 cm on the high jump to the line and across to the long jump

6 (c) Another boy has a best high jump of 195 cm

Give a reason why you should **not** use a line of best fit to estimate his best long jump.

[1 mark]

Outside the range of the data

The data goes up to 185 cm for the high jump. It is not certain that the positive correlation will continue in a straight line beyond this point

Turn over for the next question

4



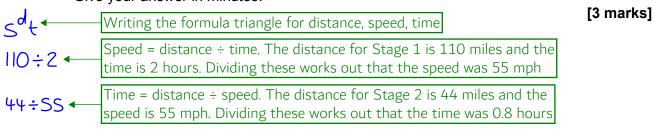
7 A car journey is in two stages.

Stage 1 The car travels 110 miles in 2 hours.

Stage 2 The car travels 44 miles at the same average speed as Stage 1

Work out the time for Stage 2

Give your answer in minutes.



Answer 48 minutes

0.8 × 60 ← There are 60 minutes in an hour so multiplying the 0.8 hours by 60 converts it into 48 minutes

8 Here is an identity.

$$a(3x - 10) \equiv 21x + 2b$$

Work out the values of a and b.

[3 marks]

Dividing both sides by 2 eliminates the 2 on the right and gets b on its own



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9 J and K are ships.

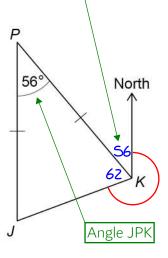
P is a port.

J is due South of P.

Angle JPK = 56°

JP = KP

This angle is alternate to angle JPK so they are equal. Line PJ goes south so is parallel to the arrow going north



Not drawn accurately

Work out the bearing of *J* from *K*.

There are 180° in total in a triangle. So subtracting angle JPK from 180° works out that there are 124° left in the triangle

[3 marks]

124÷2

The remaining two angles in the triangle are equal as the triangle must be isosceles (it has two equal sides) and these are the base angles. So the 124° can be divided by 2 to work out that each of the remaining angles are 62°

360-56-*6*2 ←

The bearing is the angle drawn in red as this is the number of degrees turned clockwise from north from K. There are 360° around a point so subtracting the two other angles around the point from 360° works out the bearing

Answer ______242

Turn over for the next question

9



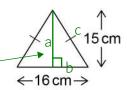
Do not write outside the box 10 The 5th term of a linear sequence is 17 The 6th term of the sequence is 21 Work out the 100th term of the sequence. [3 marks] Linear sequences change by the same amount between each term. So subtracting the 5th term from the 6th term works out that the sequence increases by 4 between each term Subtracting the 6 from 100 works out that the 100th term is 94 terms after the 6th term It must increase 94 lots of 4 between the 6th term and the 100th term. Adding 94 x 4 to the 6th term works out the 100th term Answer ____ The value of a house is £120 000 11 The value is expected to increase by 5% each year. Work out the expected value after 4 years. Give your answer to 2 significant figures. You **must** show your working. [4 marks] Adding 5% to 100% expresses the percentage it increases to each year. Putting this over 100 converts it into a fraction, which increases by 5% when multiplied by. Raising the fraction to the power of 4 as it needs to be increased by 4 times Answer £ The answer of 145860.75 is rounded to 2 significant figures



An isosceles triangle has base 16 cm and perpendicular height 15 cm

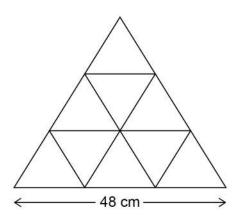
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Drawing a line down the centre of the triangle would form a right-angled triangle with base 8 cm (as this is half of the 16 cm) and height 15 cm



Not drawn accurately

Some of these triangles are used to make a large triangle.



Not drawn accurately

Work out the perimeter of the large triangle.

 $a^2+b^2=c^2$

Pythagoras' Theorem can be used to find the missing length of the right-angled triangle formed as shown above

[4 marks]

C=√15°+8° +

Square rooting both sides finds c, which is the longest side and is the one we are trying to find. Substituting 15 for a and 8 for b. So the slanted side of each small isosceles triangle is 17 cm

17×6+48**◆**

There are 6 of the slanted side on the perimeter of the large triangle so doing 17 x 6 works out the total length of these. Then adding the 48 cm which is the base. Perimeter is all of the outside sides added together

Answer

ISO

cm

11



200 people recorded the time they spent on social media one day.

The table shows the results.

Time, t (mins)	Frequency	Midpoint	
0 ≤ <i>t</i> < 30	24	IS	360
30 ≤ <i>t</i> < 50	76	40	3040
50 ≤ <i>t</i> < 60	52	55	2860
60 ≤ <i>t</i> < 90	48	75	3600
	Total = 200		9860

13 (a) Work out an estimate of the mean time.

[3 marks]

: 200

Mean = total ÷ number, where total is the total time in minutes and number is the number of people. Using the midpoint of each category to estimate the time for all of the people in each category. The midpoints can be worked out by doing the mean of the upper and lower bound of each category.

$$0 + 30 = 30$$
. Then $30 \div 2 = 15$

Multiplying the midpoints by the frequencies for each category works out an estimate of the total time for each category.

Then adding all of these totals works out that the estimated total time is 9860 minutes. Dividing this by the 200 people works out an estimate of the mean time

Answer 49.3	mins
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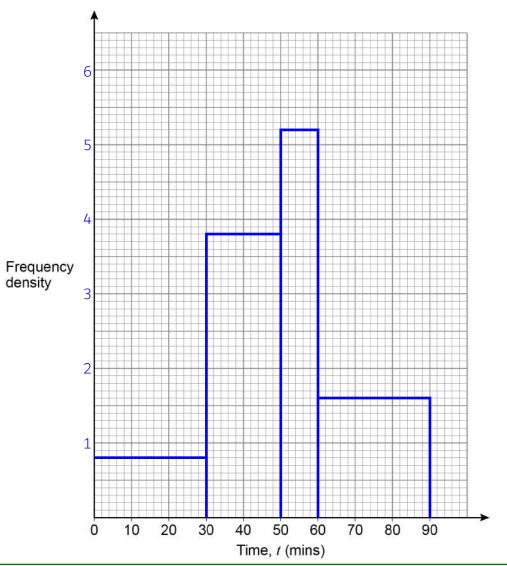


13 (b) Draw a histogram to represent the results.

Do not write outside the box

[4 marks]

Time, t (mins)	Frequency	Class width	Frequency density	
0 ≤ <i>t</i> < 30	24	30	0.8 ←	24 ÷ 30 = 0.8
30 ≤ <i>t</i> < 50	76	20	3.8 ←	76 ÷ 20 = 3.8
50 ≤ <i>t</i> < 60	52	10	5.2 ←	52 ÷ 10 = 5.2
60 ≤ <i>t</i> < 90	48	30	1.6 ←	48 ÷ 30 = 1.6



Writing a formula triangle for class width, frequency, frequency density. Class width is how wide each interval is on the graph. From the formula triangle, frequency density = frequency/class width

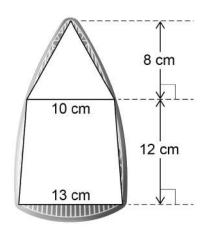


14 Ralf has an iron.

He models the base as a triangle joined to a trapezium.

Not drawn accurately





The iron applies a force of 25 newtons (N) 14 (a)

$$pressure = \frac{force}{area}$$

Work out the pressure using Ralf's model.

[4 marks]

Area of triangle =
$$1/2$$
 x base x height. The base of the triangle is $1/2 \times 10 \times 8 = 40$ $1/2 \times 10 \times 8 = 40$

Area of triangle =
$$1/2$$
 x base x height. The base of the triangle is 10 cm and the height is 8 cm. So the area of the triangle is 40 cm²

Area of triangle = $1/2$ x base x height. The base of the triangle is 10 cm and the height is 8 cm. So the area of the triangle is 40 cm²

Area of triangle = $1/2$ (a + b) x h, where a and b are the parallel sides and the h is the distance between them. a is 10 cm, b is 13 cm and h is 12 cm. So the area of the triangle is

Answer 0.14 N/cm²

14 (b) Is the actual pressure greater than, equal to or less than your answer to part (a)? Tick one box.

greater than



equal to



less than

Give a reason for your answer.

Area is greater

[2 marks]

From the diagrams, it can be seen that the area of the iron is actually greater than what it is in the model. So the force should be divided by more, which will make the pressure less

Rearrange $y = \sqrt{w^3}$ to make w the subject. 15 Circle your answer.

[1 mark]

$$w = y^6$$

$$w = \sqrt[3]{y^2}$$

$$w = \sqrt{y^3} \qquad \qquad w = y^5$$

$$w = y^{5}$$

Squaring both sides eliminates the square root on the right

Then cube rooting both sides eliminates the power of 3 and gets w on its own

Turn over for the next question

[1 mark]

16 (a) Show that a% of b = b% of a

$$\frac{a}{100} \times b = \frac{ab}{100} \leftarrow$$

Percentage is out of 100 so putting a over 100 converts the $\frac{a}{100} \times b = \frac{ab}{100}$ percentage into a fraction, which finds a% of b when multiplied by b. Simplifying the expression by multiplying the a and b

$$\frac{b}{100} \times a = \frac{ab}{100}$$

 $\frac{b}{100} \times a = \frac{ab}{100}$ Percentage is out of 100 so putting b over 100 converts the percentage into a fraction, which finds b% of a when multiplied by a Simplifying the expression by multiplying the band a by a. Simplifying the expression by multiplying the b and a

Both simplified expressions are the same, showing that the statement is correct

16 (b) Rosie says,

"160% of 40 = 140% of 60 because a% of b = b% of a"

Is she correct?

Tick a box.





Give a reason for your answer.

a is not the same in the 160% and 60

[1 mark]

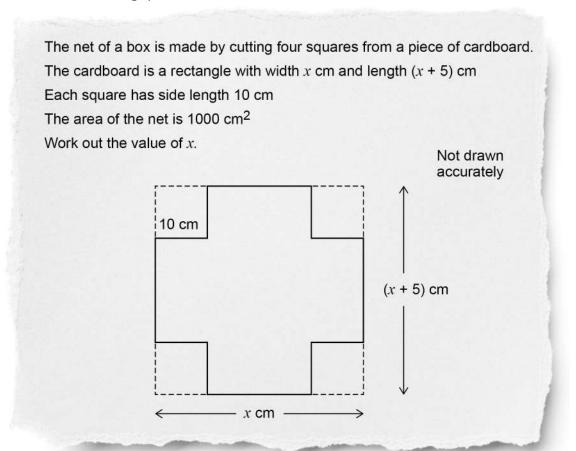


Do not write outside the box 17 A packet contains 80 sweets. The flavour of each sweet is lemon, orange or apple. A sweet is taken at random. 17 (a) $P(lemon or orange) \leq 0.85$ Work out the minimum possible number of **apple** sweets in the packet. [2 marks] The greatest probability is wanted for lemon or orange so that the probability of apple is as small as possible. The greatest this can be is 0.85. It is certain to I-0.85 **←** be apple or not apple. So subtracting the 0.85 from 1 (which is the probability of something which is certain) leaves the minimum probability of apple Multiplying the minimum probability of apple by the 80 sweets works out the minimum number of apple Answer _____ 17 (b) P(lemon or apple) < 0.71There are 31 lemon sweets. Work out the maximum possible number of **apple** sweets in the packet. [2 marks] Multiplying the upper bound of the probability of lemon or apple works out that the 0.71 x 80 ← upper bound of the number of lemon or apple is 56.8. There needs to be a whole number so rounding down to 56 means that the probability would be less than 0.71 Subtracting the 31 lemon from the 56 lemon or apple leaves 25 apple Answer ____

1 5

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18 Kate has the following question for homework.



18 (a) Show that Kate can form the equation

$$x^2 + 5x - 1400 = 0$$

[3 marks]

Area of rectangle = length x width. The length of the cardboard is x + 5 and the width is x. So multiplying these together expresses the area of the piece of cardboard. Area of square = length 2 . The length of each square is 10 so squaring this expresses the area of one of the squares. Multiplying this by 4 as there are 4 of these squares. Subtracting this as the squares are cut from the piece of cardboard

$$x^2+5x-400=1000$$

Expanding the bracket. $4 \times 10^2 = 400$. Setting the expression of the area of the net equal to the 1000 cm^2

$$x^2 + 5x - 1400 = 0$$

Subtracting 1000 from both sides gives the desired equation



18 (b) Kate correctly factorises the equation to get (x + 40)(x - 35) = 0Her answer to the homework question is x = -40 or x = 35

Is her answer correct?

Tick a box.





Give a reason for your answer.

Length cannot be negative ← x is a length

[1 mark]

19 Circle the word that describes the graph $y = \sin x$

[1 mark]



exponential

cubic

quadratic

As it repeats every 360°

20 (7, 28) is a point on the graph y = f(x)

Circle the point which **must** be on the graph y = f(x) + 2

[1 mark]

(7, 26)

(7, 30)

(5, 28)

(9, 28)

Adding 2 to the right increases y by 2. 28 + 2 = 30. The x-coordinate is not changed

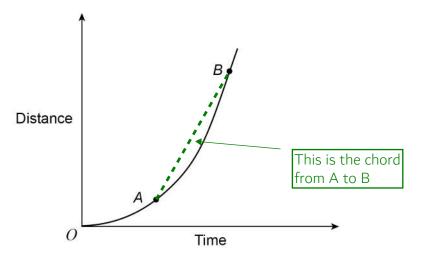
6



Simplifying by collecting like terms. n² - n² = 0. -n + n = 0. n³ must be a cube number



Here is a sketch of a distance-time graph.



Which of these represents the average speed between *A* and *B*? Tick **one** box.

[1 mark]

	The gradient of the tangent at A ←	This gives the speed at A
	The gradient of the tangent at <i>B</i> ◆	This gives the speed at B
/	The gradient of the chord from <i>A</i> to <i>B</i>	
	The gradient of the chord from O to $B \longleftarrow$	This gives the average speed from the start to B

Gradient = (change in y)/(change in x). The change in y is change in distance and the change in x is change in time. So the gradient divides the distance between A and B by the time, which gives the average speed between A and B

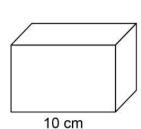
Turn over for the next question

5



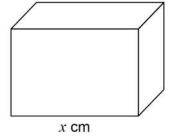
- 23 Here are three similar cuboids, A, B and C.
 - A has length 5 cm, width 2 cm and height 3 cm
 - B has length 10 cm
 - C has length x cm

Α



В

С



- 3 cm 2 cm
- 23 (a) The total surface area of A is 62 cm²

Tim wants to work out the total surface area of B.

Here is his working.

$$10 \div 5 = 2$$

$$62 \times 2 = 124$$

Total surface area of $B = 124 \text{ cm}^2$

Make **one** criticism of Tim's method.

[1 mark]

Should be 62 x 2²

 $10 \div 5$ works out that all the lengths of A have been multiplied by 2 to get the lengths of B. The unit of area is cm² so the scale factor should be squared when going from the surface area of A to the surface area of B

[3 marks]

23 (b) Volume of A ×
$$\frac{125}{8}$$
 = Volume of C

Work out the value of x.

3/<u>125</u> ◆

125/8 is the volume scale factor from A to C. The unit of volume is cm³ so cube rooting this volume scale factor gives the length scale factor

Sx2.S ← Multiplying the length of A by the length scale factor works out x

Answer I2.S

Turn over for the next question

4



	Do not write outside the box
narks]	

24 Here are two inequalities.

$$-2 \le x \le 3$$

$$9 \leqslant x + y \leqslant 11$$

x and y are integers.

Work out the **greatest** possible value of y-x

[3 m

y - x will be greatest using the upper bound of y and the lower bound of x. So x should be -2. Subtracting x from both sides of the second inequality solves for y. Just dealing with the right side and ignoring the left side of the inequality as we are looking for the upper bound of y. So y should be 13

Doing the chosen value of y subtract the chosen value of x

Answer	5

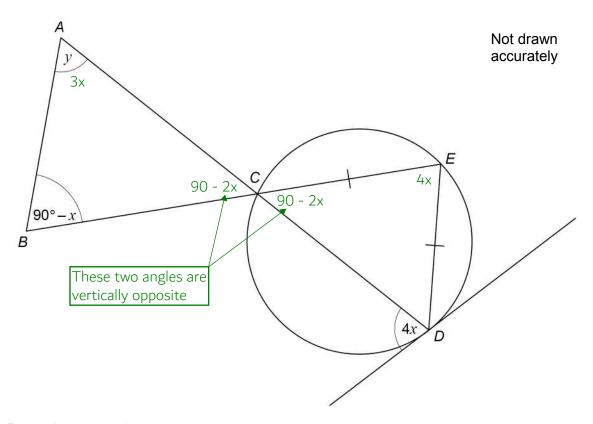


25 *C*, *D* and *E* are points on a circle.

CE = DE

The tangent at *D* is shown.

ACD and BCE are straight lines.



Prove that y = 3x

[4 marks]

Angle CED = 4x due to the alternate segment theorem.

The angle between a tangent and a chord (4x) is equal to the interior opposite angle (CED)

(180 - 4x)/2

Angle ECD = 90 - 2x as there are 180° in a triangle and the base angles of an isosceles triangle are equal.

Subtracting angle CED from 180 leaves the total of the other two angles in the triangle CED. The other two angles are equal as these are the base angles of an isosceles triangle (as it has two equal sides). So dividing 180 - 4x by 2 works out each base angle, one of these being angle ECD

Angle ACB = 90 - 2x as vertically opposite angles are equal.

$$y = 180 - (90 - x) - (90 - 2x) = 180 - 90 + x - 90 + 2x = 3x$$
 as angles in a triangle add up to 180°

Subtracting angles ABC and ACB from 180 leaves angle BAC (which is y) in the triangle ABC.

7



26 P, Q and R have positive values.

P is directly proportional to the square of Q.

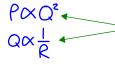
When
$$P = 1.25$$
, $Q = 0.5$

Q is inversely proportional to R.

When
$$Q = 0.5$$
, $R = 6$

Work out the value of R when P = 0.8

[5 marks]



Writing out the proportions to make it easier to visualise

 $\sqrt{\frac{0.8}{1.25}}$ ×0.5

Using the first proportion, whatever happens to P, the square root of this needs to happen to Q. P is multiplied by 0.8/1.25 so Q must be multiplied by the square root of this. So when P = 0.8, Q = 0.4

Using the second proportion, whatever happens to Q, the reciprocal of this needs to happen to R. Q is multiplied by 0.4/0.5 so R must be multiplied by the reciprocal of this



 $x_{n+1} = \sqrt[3]{3x_n + 7}$ 27

Do not write outside the box

Use a starting value of $x_1 = 2$ to work out a solution to $x = \sqrt[3]{3x+7}$

Give your answer to 3 decimal places.

[3 marks]

_		
E	ntering 2 into the calculator and pressing = (or EXE). Entering 3 3Ans + 7 and keep pressing = (or EXE) ι	until
а	If the digits in the answer stop changing. This gives 2.425988757 , which can be given to 3 decimal places	5

Answer _____ 2.426

END OF QUESTIONS

